

QUIZ 5

QUIZ 5

- (i) \neg denotes the negation
- (ii) \vee denotes the conjunction and \wedge the disjunction
- (iii) \leftrightarrow denotes the conditional

How many of the three statements above are correct?

- A.** 0
- B.** 1
- C.** 2
- D.** 3

In the following question, $(B, +, \cdot, -)$ is a Boolean algebra. The zero element is denoted by 0 and the unit element by 1.

Consider the following statements:

- (i) $+$ is idempotent
- (ii) $+$ is distributive over \cdot
- (iii) there is a neutral element for $+$
- (iv) there is an absorbing element for $+$

How many of these four statements are correct?

- A. 0
 - B. 1
 - C. 2
 - D. 3
 - E. 4
-

The converse of $p \rightarrow q$ is:

- A. $q \rightarrow p$
 - B. $(\neg p) \rightarrow (\neg q)$
 - C. $(\neg q) \rightarrow (\neg p)$
 - D. None of the above
-

The propositional expression $p \rightarrow q$ is equivalent to:

- A. $q \rightarrow p$
- B. $(\neg p) \rightarrow (\neg q)$
- C. $(\neg q) \rightarrow (\neg p)$
- D. None of the above

Consider the following statements:

- (i) \neg has higher precedence than \vee
- (ii) \vee has higher precedence than \wedge
- (iii) \wedge has higher precedence than \leftrightarrow
- (iv) \leftrightarrow has higher precedence than \rightarrow

How many of these four statements are correct?

- A. 0
- B. 1
- C. 2
- D. 3
- E. 4

Consider the following statements:

- (i) $\neg p \wedge p$ is a tautology
- (ii) $p \rightarrow p$ is a contingency
- (iii) $p \wedge p$ is a contradiction

How many of these three statements are correct?

- A.** 0
 - B.** 1
 - C.** 2
 - D.** 3
-

Let P be a binary predicate.
Assume $P(u,v)$ is the statement: "u loves v."

Which one of the propositions below corresponds to:
"Somebody loves everybody."

- A.** $\forall u, \forall v, P(u,v)$
 - B.** $\exists u, \forall v, P(u,v)$
 - C.** $\forall u, \exists v, P(u,v)$
 - D.** $\exists u, \exists v, P(u,v)$
 - E.** None of the above
-

Let P be a binary predicate.

Assume $P(u,v)$ is the statement: "u loves v."

Which one of the propositions below corresponds to:
"There is somebody who is loved by everybody."

- A. $\forall u, \forall v, P(u,v)$
- B. $\exists u, \forall v, P(u,v)$
- C. $\forall u, \exists v, P(u,v)$
- D. $\exists u, \exists v, P(u,v)$
- E. None of the above

Consider $P : \mathbb{R} \rightarrow \mathcal{P}$

$u \mapsto P(u)$ where $P(u)$ is the statement " $|u| > u$ ".

Consider the propositions below:

- (i) $\exists u \in \mathbb{R}, P(u)$
- (ii) $\exists u \in \mathbb{R}^+, P(u)$
- (iii) $\exists u \in \{\}, P(u)$

How many of these three propositions are true?

- A. 0
- B. 1
- C. 2
- D. 3

Consider $P : \mathbb{R} \rightarrow \mathcal{P}$
 $u \mapsto P(u)$ where $P(u)$ is the statement " $|u| > u$ ".

Consider the propositions below:

- (i) $\forall u \in \mathbb{R}, P(u)$
- (ii) $\forall u \in \mathbb{R}^+, P(u)$
- (iii) $\forall u \in \{\}, P(u)$

How many of these three propositions are true?

- A. 0
- B. 1
- C. 2
- D. 3

Consider the Boolean algebra $(\{0,1\}, +, \cdot, -)$ as seen in class.
 Consider the Boolean function F defined by the table below:

| x | y | z | $F(x,y,z)$ |
|-----|-----|-----|------------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

Which one of the statements below is correct?

- A. The sum-of-products expansion of F is the sum of 8 minterms.
- B. The sum-of-products expansion of F is the sum of 6 minterms.
- C. The sum-of-products expansion of F is the sum of 2 minterms.
- D. None of the above

Consider the Boolean algebra $(\{0,1\}, +, \cdot, -)$ as seen in class.
Consider the statements below:

- (i) The NOR operation is defined by: $x \downarrow y = \overline{x+y}$
- (ii) The Boolean expression \bar{x} is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (iii) The Boolean expression $x+y$ is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (iv) The Boolean expression $x \cdot y$ is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (v) $\{\downarrow\}$ is functionally complete

How many of these five statements are correct?

- A. 1
 - B. 2
 - C. 3
 - D. 4
 - E. 5
-