QUIZ 6

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Consider the Boolean algebra $(\{0,1\},+,\cdot,-)$ as seen in class. Consider the Boolean function *F* defined by the table below:

x	y	Z	F(x,y,z)
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

Which one of the statements below is correct?

- **A.** The sum-of-products expansion of *F* is the sum of 8 minterms.
- **B.** The sum-of-products expansion of *F* is the sum of 6 minterms.
- **C.** The sum-of-products expansion of *F* is the sum of 2 minterms.
- **D.** None of the above

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Consider the Boolean algebra $(\{0,1\},+,\cdot,-)$ as seen in class. Consider the statements below:

- (i) The NOR operation is defined by: $x \downarrow y = \overline{x+y}$
- (ii) The Boolean expression \overline{x} is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (iii) The Boolean expression x+y is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (iv) The Boolean expression x y is equivalent to a Boolean expression that involves no other Boolean operation than \downarrow
- (v) $\{\downarrow\}$ is functionally complete

How many of these five statements are correct?

- **A.** 1
- **B.** 2
- **C.** 3
- **D.** 4
- **E.** 5

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- **A.** We have: $\neg(\forall u, P(u)) \equiv \forall u, \neg P(u)$
- **B.** We have: $\neg(\forall u, P(u)) \equiv \exists u, P(u)$
- **C.** We have: $\neg(\forall u, P(u)) \equiv \exists u, \neg P(u)$
- **D.** None of the above

Consider the following statements:

(i) $\exists u, (P(u) \lor Q(u)) \equiv (\exists u, P(u)) \lor (\exists u, Q(u))$ (ii) $\exists u, (P(u) \land Q(u)) \equiv (\exists u, P(u)) \land (\exists u, Q(u))$

- **A.** The only correct statement is (i)
- **B.** The only correct statement is (ii)
- **C.** Both statements are correct
- **D.** None of these statements is correct

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Consider the following statements:

- (i) $\forall u, (P(u) \lor Q(u)) \equiv (\forall u, P(u)) \lor (\forall u, Q(u))$ (ii) $\forall u, (P(u) \land Q(u)) \equiv (\forall u, P(u)) \land (\forall u, Q(u))$
- **A.** The only correct statement is (i) **B.** The only correct statement is (ii)
- The only correct statement is (ii)
- **C.** Both statements are correct
- **D.** None of these statements is correct

Consider the following statements:

- (i) $\exists u, (\exists v, P(u,v)) \equiv \exists v, (\exists u, P(u,v))$
- (ii) $\forall u, (\forall v, P(u,v)) \equiv \forall v, (\forall u, P(u,v))$
- **A.** The only correct statement is (i)
- **B.** The only correct statement is (ii)
- **C.** Both statements are correct
- **D.** None of these statements is correct

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Consider the following statements:

- (i) $\exists u, (\forall v, P(u,v)) \equiv \forall v, (\exists u, P(u,v))$
- (ii) $\forall u, (\exists v, P(u,v)) \equiv \exists v, (\forall u, P(u,v))$
- **A.** The only correct statement is (i)
- **B.** The only correct statement is (ii)
- **C.** Both statements are correct
- **D.** None of these statements is correct

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Consider the following expressions:

(i)
$$(\exists v, \neg P(v)) \rightarrow (\forall v, P(u))$$

(ii) $(\exists v, \neg P(v)) \rightarrow (\forall u, P(v))$

- **A.** The only correct predicate expression is (i)
- B. The only correct predicate expression is (ii)
- **C.** Both expressions are correct predicate expressions
- **D.** None of them are correct predicate expressions

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Consider the following expressions:

- (i) $\exists u, [(\forall v, P(u,v)) \lor Q(v)]$
- (ii) $\exists u, [(\forall u, P(u, u)) \lor Q(u)]$
- **A.** The only correct predicate expression is (i)
- B. The only correct predicate expression is (ii)
- **C.** Both expressions are correct predicate expressions
- **D.** None of them are correct predicate expressions

Consider the following predicate expression:

 $\exists u, [(\forall v, P(u,v)) \lor Q(u)]$

- **A.** The scope of the existential quantifier is $[(\forall v, P(u,v)) \lor Q(u)]$
- **B.** The scope of the existential quantifier is $\forall v$, P(u,v)
- **C.** The scope of the existential quantifier is P(u,v)
- **D.** The scope of the existential quantifier is Q(u)
- **E.** None of the above